

Solomon Practice Paper

Further Pure Mathematics 3H

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	5	
2	8	
3	8	
4	12	
5	13	
6	14	
7	15	
Total:	75	

How I can achieve better:

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4. The points A, B and C have position vectors \mathbf{a}, \mathbf{b} and \mathbf{c} respectively such that

$$\mathbf{a} = 2\mathbf{i} - \mathbf{j} + \mathbf{k} \quad \text{and} \quad \mathbf{b} = \mathbf{i} + q\mathbf{j} - 3\mathbf{k} \quad \text{and} \quad \mathbf{c} = 3\mathbf{i} - 4\mathbf{j} + 5\mathbf{k}$$

where q is a constant and $q \neq 2$.

(a) Find $\overrightarrow{AB} \times \overrightarrow{AC}$, giving your answer in terms of q . [5]

(b) Hence show that the vector $\mathbf{n} = 4\mathbf{i} - \mathbf{k}$ is perpendicular to the plane Π containing A, B and C for all real values of q . [2]

(c) Find an equation of the plane Π , giving your answer in the form $\mathbf{r} \cdot \mathbf{n} = p$. [2]

Given that $q = -1$,

(d) find the volume of the tetrahedron $OABC$. [3]

Total: 12



7.

$$\mathbf{A} = \begin{pmatrix} 2 & a & 2 \\ -1 & b & -2 \\ 0 & 0 & c \end{pmatrix} \quad \text{and} \quad \mathbf{B} = \begin{pmatrix} 6 & 5 & 2 \\ -1 & 0 & -2 \\ 0 & 0 & 5 \end{pmatrix}$$

and

$$(\mathbf{B} - 2\mathbf{I})\mathbf{A} = 3\mathbf{I} \quad (\star)$$

where a, b and c are constants and \mathbf{I} is the 3×3 identity matrix.

(a) Find the values of a, b and c . [6]

(b) Using equation (\star) , or otherwise, find \mathbf{A}^{-1} , showing your working clearly. [2]

The transformation $T : \mathbb{R}^3 \rightarrow \mathbb{R}^3$ is represented by the matrix \mathbf{A} .

(c) Find an equation satisfied by all the points which remain invariant under T . [4]

T maps the vector $\begin{pmatrix} p \\ q \\ r \end{pmatrix}$ onto the vector $\begin{pmatrix} 4 \\ -5 \\ 3 \end{pmatrix}$.

(d) Find the values of p, q and r . [3]

Total: 15

