

Solomon Practice Paper

Further Pure Mathematics 3D

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	7	
2	9	
3	10	
4	11	
5	11	
6	13	
7	14	
Total:	75	

How I can achieve better:

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2. The variable y satisfies the differential equation

$$\frac{dy}{dx} = x^2 + y + 2, \quad y = 0 \quad \text{at} \quad x = 0.$$

(a) Given that $y \approx 2h$ when $x = h$, use the approximation [4]

$$\left(\frac{dy}{dx}\right)_0 \approx \frac{y_1 - y_{-1}}{2h}$$

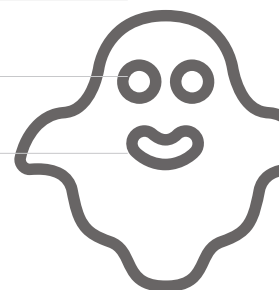
once to obtain an estimate for y as a function of h when $x = 2h$.

(b) Use the same approximation to show that an estimate for y when $x = 3h$ is given by [3]

$$y \approx 2h(2h^3 + 8h^2 + 4h + 3).$$

(c) Hence find an estimate for y when $x = 0.3$. [2]

Total: 9



5. The transformation $T : \mathbb{R}^3 \rightarrow \mathbb{R}^3$ is represented by the matrix \mathbf{A} where

$$\mathbf{A} = \begin{pmatrix} 2 & a & 1 \\ 1 & 2 & -1 \\ 3 & 1 & 1 \end{pmatrix}$$

- (a) Find \mathbf{A}^{-1} , showing your working clearly and stating the condition for which \mathbf{A} is non-singular. [7]

Relative to a fixed origin O , the transformation T maps the point P onto the point Q .

When $a = -1$, Q has position vector $5\mathbf{i} - 4\mathbf{j} + 2\mathbf{k}$.

- (b) Find the position vector of P , showing your working clearly. [4]

Total: 11



7. The transformation T from the complex z -plane to the complex w -plane is given by

$$w = \frac{1}{z^* - 2}, \quad z \neq 2.$$

- (a) Show that the image in the w -plane of the line $\Re(z) = 5$ in the z -plane, under T , is a circle. [7]
Find its centre and radius.

The region represented by $\Re(z) > 5$ in the z -plane is transformed under T into the region represented by R in the w -plane.

- (b) Show the region R on an Argand diagram. [3]

- (c) Find the image in the w -plane under T of the half-line $\arg(z - 2) = \frac{\pi}{4}$ in the z -plane. [4]

Total: 14

