

Solomon Practice Paper

Further Pure Mathematics 3C

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	6	
2	7	
3	10	
4	11	
5	11	
6	14	
7	16	
Total:	75	

How I can achieve better:

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6. The eigenvalues of the matrix

$$\mathbf{M} = \begin{pmatrix} 2 & -1 & 1 \\ -1 & 0 & 1 \\ 1 & 1 & 2 \end{pmatrix}$$

are λ_1, λ_2 and λ_3 .

(a) Show that $\lambda_1 = 2$ is an eigenvalue of \mathbf{M} and find the other two eigenvalues λ_2 and λ_3 . [7]

(b) Find an eigenvector corresponding to the eigenvalue 2. [4]

Given that $\begin{pmatrix} 1 \\ 2 \\ -1 \end{pmatrix}$ and $\begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$ are eigenvectors of \mathbf{M} corresponding to λ_2 and λ_3 respectively,

(c) write down a matrix \mathbf{P} such that [3]

$$\mathbf{P}^{-1}\mathbf{M}\mathbf{P} = \begin{pmatrix} \lambda_1 & 0 & 0 \\ 0 & \lambda_2 & 0 \\ 0 & 0 & \lambda_3 \end{pmatrix}.$$

Total: 14



