

# Solomon Practice Paper

## Further Pure Mathematics 2C

Time allowed: 90 minutes

Centre: [www.CasperYC.club](http://www.CasperYC.club)

Name:

Teacher:

Question	Points	Score
1	5	
2	7	
3	10	
4	12	
5	12	
6	13	
7	16	
Total:	75	

How I can achieve better:

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5.

$$f(x) = \operatorname{arctanh}\left(\frac{x^2 - 1}{x^2 + 1}\right), \quad x > 0.$$

(a) Using the definitions of  $\sinh(x)$  and  $\cosh(x)$  in terms of exponentials, express  $\tanh(x)$  in terms of  $e^x$  and  $e^{-x}$ . [1]

(b) Hence prove that [6]

$$f(x) = \ln(x).$$

(c) Hence, or otherwise, show that the area bounded by the curve  $y = \operatorname{arctanh}\left(\frac{x^2-1}{x^2+1}\right)$ , the positive  $x$ -axis and the line  $x = 2e$  is  $2e \ln(2) + 1$ . [5]

Total: 12



6. The ellipse  $C$  has equation

$$\frac{x^2}{25} + \frac{y^2}{9} = 1.$$

(a) Find an equation of the normal to  $C$  at the point  $P(5 \cos \theta, 3 \sin \theta)$ . [5]

The normal to  $C$  at  $P$  meets the coordinate axes at  $Q$  and  $R$ .

Given that  $ORSQ$  is a rectangle, where  $O$  is the origin,

(b) show that, as  $\theta$  varies, the locus of  $S$  is an ellipse and find its equation in Cartesian form. [8]

Total: 13



