

Solomon Practice Paper

Further Pure Mathematics 1H

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	6	
2	8	
3	9	
4	9	
5	10	
6	15	
7	18	
Total:	75	

How I can achieve better:

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Last updated:

December 24, 2025



4.

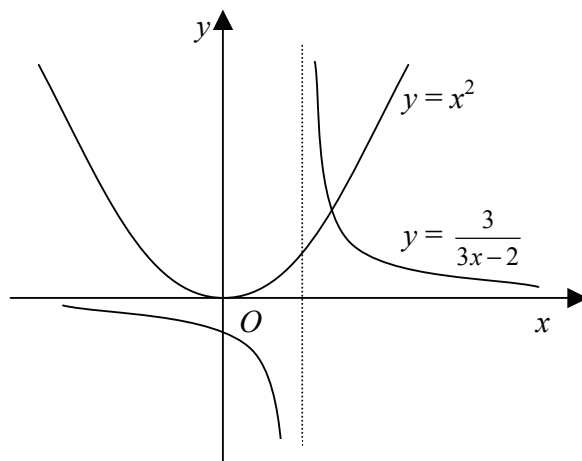


Figure above shows part of the curves $y = x^2$ and $y = \frac{3}{3x-2}$.
The curves meet at the point with x -coordinate α .

(a) Find the integer N such that

$$\frac{N}{10} < \alpha < \frac{N+1}{10}.$$

[4]

(b) Use interval bisection on the interval found in part (a) to find the value of α correct to 2 decimal places.

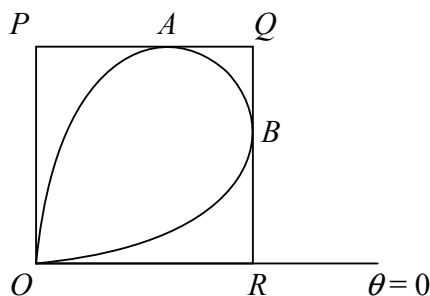
[5]

Total: 9



6. The shape of a company logo is to be the region enclosed by the curve with polar equation

$$r^2 = a^2 \sin(2\theta), \quad 0 \leq \theta \leq \frac{\pi}{2}.$$



A sign in the shape of the logo is to be made by cutting the area enclosed by the curve from a square sheet of metal $OPQR$ where O is the pole and R lies on the initial line, $\theta = 0$, as shown.

PQ and QR are tangents to the curve, parallel and perpendicular to the initial line respectively, at the points A and B on the curve.

(a) Find the value of θ at the point A . [7]

(b) Show that the area of $OPQR$ is $\frac{3\sqrt{3}}{8}a^2$. [3]

(c) Find the area of the metal sheet which is not used. [5]

Total: 15



7. Given that $x = ke^{-t}$ satisfies the differential equation

$$\frac{d^2x}{dt^2} + 5\frac{dx}{dt} + 6x = 8e^{-t},$$

(a) find the value of k . [3]

(b) Hence find the solution of the differential equation for which $x = 1$ and $\frac{dx}{dt} = 3$ at $t = 0$. [8]

The maximum value of x occurs when $t = T$.

(c) Show that the maximum value of x is $\frac{40}{27}$ and find the value of T . [7]

Total: 18

