

Solomon Practice Paper

Core Mathematics 4G

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	6	
2	7	
3	8	
4	9	
5	9	
6	10	
7	11	
8	15	
Total:	75	

How I can achieve better:

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-
-



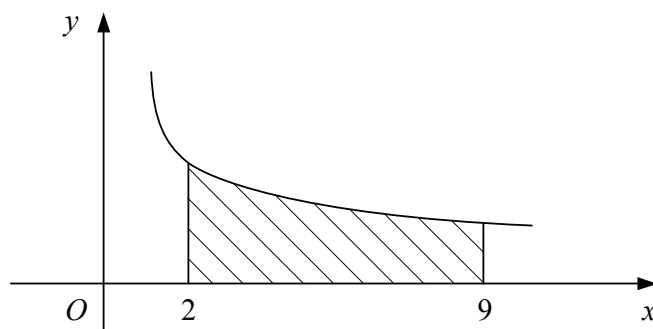
Last updated:

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7. Figure shows the curve with parametric equations

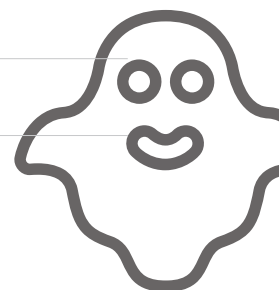
$$x = t^3 + 1, \quad \text{and} \quad y = \frac{2}{t}, \quad t > 0.$$



The shaded region is bounded by the curve, the x -axis and the lines $x = 2$ and $x = 9$.

- (a) Find the area of the shaded region. [5]
- (b) Show that the volume of the solid formed when the shaded region is rotated through 2π radians about the x -axis is 12π . [3]
- (c) Find a Cartesian equation for the curve in the form $y = f(x)$. [3]

Total: 11



8. (a) Show that the substitution $u = \sin(x)$ transforms the integral

[4]

$$\int \frac{6}{\cos(x)(2 - \sin(x))} dx$$

into the integral

$$\int \frac{6}{(1 - u^2)(2 - u)} du.$$

(b) Express

[4]

$$\frac{6}{(1 - u^2)(2 - u)}$$

in partial fractions.

(c) Hence, evaluate

[7]

$$\int_0^{\frac{\pi}{6}} \frac{6}{\cos(x)(2 - \sin(x))} dx,$$

giving your answer in the form $a \ln(2) + b \ln(3)$, where a and b are integers.

Total: 15

