

Solomon Practice Paper

Core Mathematics 4F

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	8	
2	8	
3	9	
4	9	
5	11	
6	13	
7	17	
Total:	75	

How I can achieve better:

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-
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Last updated:

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3. (a) Show that

[2]

$$\left(1 - \frac{1}{24}\right)^{-\frac{1}{2}} = k\sqrt{6}$$

where k is rational.

(b) Expand

[4]

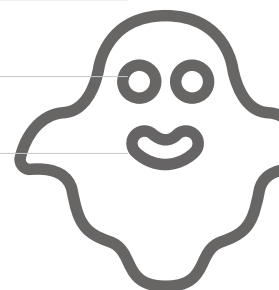
$$\left(1 + \frac{1}{2}x\right)^{-\frac{1}{2}}, \quad |x| < 2,$$

in ascending powers of x up to and including the term in x^3 , simplifying each coefficient.

(c) Use your answer to part (b) with $x = \frac{1}{12}$ to find an approximate value for $\sqrt{6}$, giving your answer to 5 decimal places.

[3]

Total: 9



5. A curve has parametric equations

$$x = \frac{t}{2-t}, \quad \text{and} \quad y = \frac{1}{1+t}, \quad -1 < t < 2.$$

(a) Show that

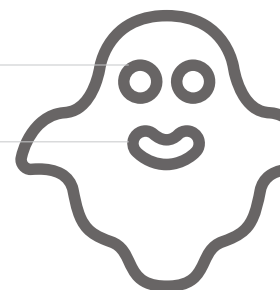
$$\frac{dy}{dx} = -\frac{1}{2} \left(\frac{2-t}{1+t} \right)^2.$$

(b) Find an equation for the normal to the curve at the point where $t = 1$.

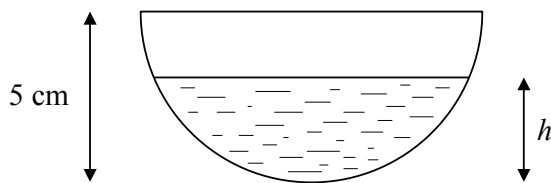
(c) Show that the cartesian equation of the curve can be written in the form

$$y = \frac{1+x}{1+3x}.$$

Total: 11



7. Figure shows a hemispherical bowl of radius 5 cm.



The bowl is filled with water but the water leaks from a hole at the base of the bowl. At time t minutes, the depth of water is h cm and the volume of water in the bowl is V cm³, where

$$V = \frac{1}{3}\pi h^2(15 - h).$$

In a model it is assumed that the rate at which the volume of water in the bowl decreases is proportional to V .

(a) Show that

$$\frac{dh}{dt} = -\frac{kh(15 - h)}{3(10 - h)},$$

where k is a positive constant.

(b) Express

$$\frac{3(10 - h)}{h(15 - h)}$$

in partial fractions.

Given that when $t = 0, h = 5$,

(c) show that

$$h^2(15 - h) = 250e^{-kt}.$$

Given also that when $t = 2, h = 4$,

(d) find the value of k to 3 significant figures.

Total: 17

