

Page 4	Mark Scheme	Syllabus	Paper
	Cambridge International A Level – October/November 2014	9709	33

- 1 Either State or imply non-modular inequality $(3x-1)^2 < (2x+5)^2$ or corresponding quadratic equation or pair of linear equations $3x-1 = \pm(2x+5)$ B1
 Solve a three-term quadratic or two linear equations $5x^2 - 26x - 24 < 0$ M1
 Obtain $-\frac{4}{5}$ and 6 A1
 State $-\frac{4}{5} < x < 6$ A1
- Or Obtain value 6 from graph, inspection or solving linear equation B1
 Obtain value $-\frac{4}{5}$ similarly B2
 State $-\frac{4}{5} < x < 6$ B1 [4]
- 2 Use correct product rule or correct chain rule to differentiate y M1
 Use $\frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}}$ M*1
 Obtain $\frac{-4 \cos \theta \sin^2 \theta + 2 \cos^3 \theta}{\sec^2 \theta}$ or equivalent A1
 Express $\frac{dy}{dx}$ in terms of $\cos \theta$ DM*1
 Confirm given answer $6 \cos^5 \theta - 4 \cos^3 \theta$ legitimately A1 [5]
- 3 (i) Either Equate $p(-1)$ or $p(-2)$ to zero or divide by $(x+1)$ or $(x+2)$ and M*1
 equate constant remainder to zero.
 Obtain two equations $a-b=6$ and $4a-2b=34$ or equivalents A1
 Solve pair of equations for a or b DM*1
 Obtain $a=11$ and $b=5$ A1
- Or State or imply third factor is $4x-1$ B1
 Carry out complete expansion of $(x+1)(x+2)(4x-1)$ or M1
 $(x+1)(x+2)(Cx+D)$
 Obtain $a=11$ A1
 Obtain $b=5$ A1 [4]
- (ii) Use division or equivalent and obtaining linear remainder M1
 Obtain quotient $4x+a$, following their value of a A1
 Indicate remainder $x-13$ A1 [3]

Page 5	Mark Scheme	Syllabus	Paper
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4	(i) <u>Either</u> Use $\cos(A \pm B)$ correctly at least once State correct complete expansion Confirm given answer $\cos \theta$ with explicit use of $\cos 60^\circ = \frac{1}{2}$ SR: “correct” answer from sign errors in both expansions is B1 only		M1 A1 A1
	<u>Or</u> Use correct $\cos A + \cos B$ formula State correct result e.g. $2 \cos\left(\frac{2\theta}{2}\right) \cos\left(\frac{-120}{2}\right)$ Confirm given answer $\cos \theta$ with explicit use of $\cos(\pm 60^\circ) = \frac{1}{2}$		M1 A1 A1 [3]
	(ii) State or imply $\frac{\cos 2x}{\cos x} = 3$ Obtain equation $2 \cos^2 x - 3 \cos x - 1 = 0$ Solve a three-term quadratic equation for $\cos x$ Obtain $\frac{1}{4}(3 - \sqrt{17})$ or exact equivalent and, finally, no other		B1 B1 M1 A1 [4]
5	(i) State or imply $iw = -3 + 5i$ Carry out multiplication by $\frac{4-i}{4-i}$ Obtain final answer $-\frac{7}{17} + \frac{23}{17}i$ or equivalent		B1 M1 A1 [3]
	(ii) Multiply w by z to obtain $17 + 17i$ State $\arg w = \tan^{-1} \frac{3}{5}$ or $\arg z = \tan^{-1} \frac{1}{4}$ State $\arg wz = \arg w + \arg z$ Confirm given result $\tan^{-1} \frac{3}{5} + \tan^{-1} \frac{1}{4} = \frac{1}{4}\pi$ legitimately		B1 B1 M1 A1 [4]
6	(i) State or imply correct ordinates 1, 0.94259..., 0.79719..., 0.62000... Use correct formula or equivalent with $h = 0.1$ and four y values Obtain 0.255 with no errors seen		B1 M1 A1 [3]
	(ii) Obtain or imply $a = -6$ Obtain x^4 term including correct attempt at coefficient Obtain or imply $b = 27$ <u>Either</u> Integrate to obtain $x - 2x^3 + \frac{27}{5}x^5$, following their values of a and b Obtain 0.259		B1 M1 A1 B1 ^b B1
	<u>Or</u> Use correct trapezium rule with at least 3 ordinates Obtain 0.259 (from 4)		M1 A1 [5]

Page 6	Mark Scheme	Syllabus	Paper
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7	(i) State at least two of the equations $1 + \lambda = a + \mu$, $4 = 2 + 2\mu$, $-2 + 3\lambda = -2 + 3a\mu$ Solve for λ or for μ Obtain $\lambda = a$ (or $\lambda = a + \mu - 1$) and $\mu = 1$ Confirm values satisfy third equation		B1 M1 A1 A1 [4]
	(ii) State or imply point of intersection is $(a+1, 4, 3a-2)$ Use correct method for the modulus of the position vector and equate to 9, following their point of intersection Solve a three-term quadratic equation in a ($a^2 - a - 6 = 0$) Obtain -2 and 3		B1 M*1 DM*1 A1 [4]
8	(i) Sensibly separate variables and attempt integration of at least one side Obtain $2y^{\frac{1}{2}} = \dots$ or equivalent Correct integration by parts of $x \sin \frac{1}{3}x$ as far as $ax \cos \frac{1}{3}x \pm \int b \cos \frac{1}{3}x dx$ Obtain $-3x \cos \frac{1}{3}x + \int 3 \cos \frac{1}{3}x dx$ or equivalent Obtain $-3x \cos \frac{1}{3}x + 9 \sin \frac{1}{3}x$ or equivalent Obtain $y = \left(-\frac{3}{10}x \cos \frac{1}{3}x + \frac{9}{10} \sin \frac{1}{3}x + c \right)^2$ or equivalent		M1 A1 M1 A1 A1 A1 [6]
	(ii) Use $x = 0$ and $y = 100$ to find constant Substitute 25 and calculate value of y Obtain 203		M*1 DM*1 A1 [3]
9	(i) Sketch increasing curve with correct curvature passing through origin, for $x \geq 0$ Recognisable sketch of $y = 40 - x^3$, with equation stated, for $x > 0$ Indicate in some way the one intersection, dependent on both curves being roughly correct and both existing for some $x < 0$		B1 B1 B1 [3]
	(ii) Consider signs of $x^3 + \ln(x+1) - 40$ at 3 and 4 or equivalent or compare values of relevant expressions for $x = 3$ and $x = 4$ Complete argument correctly with correct calculations (-11.6 and 25.6)		M1 A1 [2]
	(iii) Use the iterative formula correctly at least once Obtain final answer 3.377 Show sufficient iterations to justify accuracy to 3 d.p. or show sign change in interval (3.3765, 3.3775)		M1 A1 A1 [3]
	(iv) Attempt value of $\ln(x+1)$ Obtain 1.48		M1 A1 [2]

Page 7	Mark Scheme	Syllabus	Paper
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- 10 State or imply $\frac{du}{dx} = e^x$ B1
- Substitute throughout for x and dx M1
- Obtain $\int \frac{u}{u^2 + 3u + 2} du$ or equivalent (ignoring limits so far) A1
- State or imply partial fractions of form $\frac{A}{u+2} + \frac{B}{u+1}$, following their integrand B1
- Carry out a correct process to find at least one constant for their integrand M1
- Obtain correct $\frac{2}{u+2} - \frac{1}{u+1}$ A1
- Integrate to obtain $a \ln(u+2) + b \ln(u+1)$ M1
- Obtain $2 \ln(u+2) - \ln(u+1)$ or equivalent, follow their A and B A1✓
- Apply appropriate limits and use at least one logarithm property correctly M1
- Obtain given answer $\ln \frac{8}{5}$ legitimately A1 [10]
- SR** for integrand $\frac{u^2}{u(u+1)(u+2)}$
- State or imply partial fractions of form $\frac{A}{u} + \frac{B}{u+1} + \frac{C}{u+2}$ (B1)
- Carry out a correct process to find at least one constant (M1)
- Obtain correct $\frac{2}{u+2} - \frac{1}{u+1}$ (A1)
- ...complete as above.