

| Question | Answer | Marks |
|----------|--|-----------|
| 1 | $N(242.4, 162.24)$ | B1 |
| | $\frac{220 - '242.4'}{\sqrt{'162.24'}} (= -1.759)$ | M1 |
| | $\phi(' -1.759) = 1 - \phi('1.759) = 0.0393$ | M1 |
| | 3.93% | A1 |
| | | 4 |

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|----------|---|-----------|
| 2(a) | H_0 : Proportion = 0.05 H_1 : Proportion > 0.05 | B1 |
| | | 1 |
| 2(b) | $1 - (0.95^{25} + 25 \times 0.95^{24} \times 0.05 + {}^{25}C_2 \times 0.95^{23} \times 0.05^2 + {}^{25}C_3 \times 0.95^{22} \times 0.05^3)$ | M1 |
| | Completely correct expression | A1 |
| | 0.0341 | A1 |
| | | 3 |
| 2(c) | Type II | B1 |
| | Will conclude proportion not increased | B1 |
| | | 2 |

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|-----------|---|-----------|
| 3(a)(i) | B(3600, 0.0012) | B1 |
| | | 1 |
| 3(a)(ii) | Po(4.32) (B1 for Po. B1 for $\lambda = 4.32$) | B2 |
| | $n = 3600$ which is large, $p = 0.12$ which is small and $np = 4.32$ which is < 5 | B1 |
| | | 3 |
| 3(a)(iii) | $1 - e^{-4.32} \left(1 + 4.32 + \frac{4.32^2}{2} \right)$ | M1 |
| | 0.805 (3 sf) | A1 |
| | | 2 |
| 3(b) | $e^{-\lambda} > 0.1$ | M1 |
| | $(-\lambda > \ln 0.1)$ $(\lambda < \ln 10)$ $0.0012n < \ln 10$ | A1 |
| | $(n < 1918.8)$ largest n is 1918 | A1 |
| | | 3 |

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| 4(a) | $E(X) = 2$ | B1 |
| | $0.2 \times 1 + 0.4 \times 2^2 + 0.2 \times 3^2 + 0.1 \times 4^2 - 2^2 (= 1.2)$ AG | B1 |
| | | 2 |
| 4(b) | $\frac{a-2}{\sqrt{1.2 \div 200}} = \phi^{-1}(0.9)$ (M1 for LHS, M1 for RHS) | M1 |
| | $a = 2 + \sqrt{1.2 \div 200} \times 1.282$ | M1 |
| | 2.10 (3 sf) | A1 |
| | | 4 |
| | | |
| 4(c) | Yes, because X is not normally distributed. | B1 |
| | | 1 |
| 4(d) | H_0 : pop mean = 2 H_1 : pop mean < 2 | B1 |
| | $\frac{1.86 - 2}{\sqrt{1.2 \div 200}}$ | M1 |
| | 1.807 | A1 |
| | comp $z = 1.645$ | M1 |
| | There is evidence that the spinner is biased so that mean is less than 2 | A1 |
| | | 5 |

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| 5(a)(i) | 0, 1, 2, 3, | B1 |
| | | 1 |
| 5(a)(ii) | 3 | B1 |
| | | 1 |
| 5(a)(iii) | $e^{-3} \left(\frac{3^4}{4!} + \frac{3^5}{5!} + \frac{3^6}{6!} \right)$ | M1 |
| | 0.319 (3 sf) | A1 |
| | | 2 |
| 5(b) | $\Phi^{-1}(0.0668) (= -1.500)$ | M1 |
| | $N(\mu, \mu)$ | M1 |
| | $\frac{45.5 - \mu}{\sqrt{\mu}} = \text{“} -1.500 \text{”}$ | M1 |
| | $\mu - \text{“} -1.500 \text{”} \sqrt{\mu} - 45.5 = 0$ $\sqrt{\mu} = \frac{\text{“} -1.5 \text{”} \pm \sqrt{(\text{“} -1.5 \text{”})^2 + 4 \times 45.5}}{2} (= 7.5369)$ | M1 |
| | $\mu = 56.8$ (3 sf) | A1 |
| | | 5 |

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| 6(a) | $\int_1^a \frac{k}{x^2} dx = 1$ | M1 |
| | $k \left[-\frac{1}{x} \right]_1^a = 1$ $k \left[1 - \frac{1}{a} \right] = 1$ | A1 |
| | $k \left[\frac{a-1}{a} \right] = 1$ $\left(k = \frac{1}{a-1} \right)$ AG | A1 |
| | | 3 |
| 6(b) | $\frac{a}{a-1} \int_1^a \frac{1}{x} dx$ | M1 |
| | $\frac{a}{a-1} [\ln x]_1^a$ | A1 |
| | $\frac{a \ln a}{a-1}$ | A1 |
| | | 3 |

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| 6(c) | $\frac{a}{a-1} \int_1^m \frac{1}{x^2} dx = \frac{3}{5}$ | M1 |
| | $\frac{a}{a-1} \left[-\frac{1}{x} \right]_1^m = \frac{3}{5}$ $\frac{a}{a-1} \left[1 - \frac{1}{m} \right] = \frac{3}{5}$ | A1 |
| | $\frac{1}{m} = 1 - \frac{3(a-1)}{5a} \text{ or } \frac{1}{m} = \frac{2a+3}{5a}$ | A1 |
| | $m = \frac{5a}{2a+3}$ | A1 |
| | | 4 |