

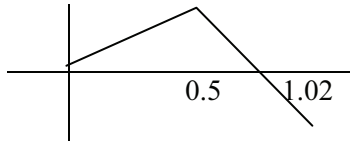
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|---|------|--|
| 1 | M1 | For using $WD = Fd \cos \alpha$ |
| $WD = 6 \times (0.5 \times 8) \cos 24^\circ$ | A1 | |
| Work done is 21.9 J | A1 | [3] |
| 2 (i) | M1 | For resolving forces horizontally or vertically |
| $T \cos \theta + T \sin \theta = 11.2$ (or $-T \cos \theta + T \sin \theta = 0.16g$) | A1 | |
| $-T \cos \theta + T \sin \theta = 0.16g$ (or $T \cos \theta + T \sin \theta = 11.2$) | A1 | [3] |
| (ii) [$T \cos \theta = 4.8$ and $T \sin \theta = 6.4$ and $T^2 = 4.8^2 + 6.4^2$ or $\tan \theta = 6.4/4.8$] [$4T^2(\cos^2 \theta + \sin^2 \theta) =$ $(11.2 - 1.6)^2 + (11.2 + 1.6)^2$ or $2T \sin \theta \div 2T \cos \theta =$ $(11.2 + 1.6) \div (11.2 - 1.6)$ or $(T \cos \theta + T \sin \theta) \div (-T \cos \theta + T \sin \theta)$ $= 11.2 \div 1.6$] | M1 | For finding $T \cos \theta$ and $T \sin \theta$ and hence finding T or θ , OR for finding the value of $4T^2(\cos^2 \theta + \sin^2 \theta)$ or of $2T \sin \theta \div 2T \cos \theta$ or of $(T \cos \theta + T \sin \theta) \div (-T \cos \theta + T \sin \theta)$ |
| $T = 8$ (or $\theta = 53.1$) | A1 | |
| $\theta = 53.1$ or $T = 8$ | A1 | [3] |
| 3 (i) | M1 | For using $s = \int v dt$ |
| $s = 0.027(10t^3/3 - t^4/4) \quad (+C)$ | A1 | |
| $s = 0.027[10\,000/3 - 10000/4]$ | DM1 | For finding the value of t at A and using limits or equivalent |
| Distance is 22.5 m | A1 | [4] |
| (ii) [$0.027(20t - 3t^2) = 0 \rightarrow t = 20/3$] | M1 | For using $dv/dt = 0$ |
| $v_{\max} = 0.027(4000/9 - 8000/27)$ | A1ft | ft incorrect t in $0.027(10t^2 - t^3)$ |
| Maximum speed is 4 ms^{-1} | A1 | [3] |

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| 4 (i) | [When $4 < v < 6$, $a_{\text{ave}} = (6 - 4)/(0.5 - 0)$; when $19 < v < 21$ $a_{\text{ave}} = (21 - 19)/(24.5 - 16.3)$] | M1 | | For using $a \approx \frac{\Delta v}{\Delta t}$ |
| | Average accelerations are 4 ms^{-2} and 0.244 ms^{-2} | A1 | [2] | |
| (ii) | DF(5) = P/5 and DF(20) = P/20 | B1 | | |
| | [DF – R = ma] | M1 | | For using Newton's 2 nd law |
| | P/5 – R = 1230 × 4 and P/20 – R = 1230 × 0.244 | A1ft | | ft incorrect average a values |
| | P = 30800 (or R = 1240) | B1 | | |
| | R = 1240 (or P = 30800) | B1ft | [5] | ft P/5 – 1230a ₁ or P/20 – 1230a ₂ or 5(1230a ₁ + R) or 20(1230a ₂ + R) |
| 5 (i) | WD against resistance = 800 × 500 | B1 | | |
| | [2800 000 = PE gain + 400 000] | M1 | | For using WD by the driving force = PE gain + WD against resistance |
| | [2400 000 = 16000g × 500sin α] | M1 | | For using PE gain = mgLsin α |
| | α = 1.7 | A1 | [4] | |
| (ii) | [KE gain = 2400 000 + 2400 000 – 800 000] | M1 | | For using KE gain = WD by the driving force + PE loss – WD against resistance |
| | 4000 000 J | A1ft | | ft PE gain |
| | [½ 16000(v ² – 20 ²) = 4000 000] | M1 | | For KE gain = ½ m(v ² – 20 ²) and attempting to solve for v |
| | Speed is 30 ms ⁻¹ | A1 | [4] | |
| SR (max 2/4) for candidates who assume constant driving force and constant resistance without justification | | | | |
| Uses Newton's Second Law and $v^2 = u^2 + 2as$ [4800 + 16000gsin α – 1600 = 16000a, $v^2 = 20^2 + 2a \times 500$] M1 Speed is 30 ms ⁻¹ A1 | | | | |
| Alternative Method for Part (i) | | | | |
| (i) | Driving force = 2800 000 ÷ 500 | B1 | | |
| | [DF – mgsinα – R = m × 0] | M1 | | |
| | For using Newton's second law | | | |
| | [16000 × 10sinα = 5600 – 800] | DM1 | | |
| | For solving the resultant equation for α | A1 | | |
| α = 1.7 | | [4] | | |

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| 6 (i) | | M1 | | For resolving forces parallel to the plane |
| | $F = 5.9 - 6.1 \sin \alpha$ | A1 | | |
| | $R = 6.1 \cos \alpha$ | B1 | | |
| | $[5.9 - 6.1 \sin \alpha \leq \mu (6.1 \cos \alpha)]$ | M1 | | For using $F \leq \mu R$ |
| | $\mu > \frac{4}{5}$ | A1 | [5] | AG |
| (ii) | $[6.1 \times (11/61) + 5.9 - \mu 6.1 \times (60/61) > 0]$ | M1 | | For using $F = \mu R$ and 'net downward force > 0' |
| | $\mu < \frac{7}{6}$ | A1 | [2] | AG |
| (iii) | $[6.1 \times (11/61) + 5.9 - \mu 6.1 \times (60/61) = 0.61 \times 1.7]$ | M1 | | For using Newton's 2 nd law and $F = \mu R$ |
| | $\mu = 0.994$ | A1 | [2] | |
| 7 (i) | | | | For using Newton's second law |
| | $[T - 0.12g = 0.12a \text{ \& } 0.38g - T = 0.38a;$ $a = \frac{0.38 - 0.12}{0.38 + 0.12} g]$ | M1 | | for A and B or for using $a = \frac{M - m}{M + m} g$ |
| | Acceleration is 5.2 ms^{-2} | A1 | [2] | |
| (ii) | $[v^2 = 2 \times 5.2 \times 0.65; 0.65 = \frac{1}{2} 5.2 T_B^2]$ | M1 | | For using $v^2 = 2ah$ or $s = \frac{1}{2} at^2$ |
| | Speed of B is 2.6 ms^{-1} or $T_B = 0.5$ | A1ft | | ft incorrect a |
| | $T_B = 0.5$ or Speed of B is 2.6 ms^{-1} | B1 | [3] | |
| (iii) | $[-2.6 = 2.6 - 10(T - 0.5)]$ | M1 | | For using $-V = V - g(T - T_B)$ or equivalent |
| | $T = 1.02$ | A1ft | | ft incorrect V and/or T_B |
| | Correct graph for $0 < t < 1.02$ ft incorrect values of V, T and T_B | B1ft | [3] |  |
| (iv) | $[0.65 + 0.5(1.02 - 0.5)2.6]$ | M1 | | For using 'total distance $= \frac{1}{2} (VT_B) + 2 \times \frac{1}{2} \frac{T_A - T_B}{2} V$ |
| | Total distance is 1.326 m (accept 1.33) | A1 | [2] | |